

# HOW A LEAP YEAR WORKS



**TEJA TEPPALA**

# About me

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- **Teja Teppala**
- **Doctoral Candidate in Astronomy**
- **Studies star formation in low-mass galaxies**



**Any leap day babies in the house?**



**Any leap day babies in the house?**



**Chances are about one in 1461!**



**What is a year, anyway?**



# Different definitions of a year



# Different definitions of a year

- **Calendar year: 365 days (or 366 days in leap years)**



# Different definitions of a year





# Different definitions of a year



- **Tropical year: time that the Sun takes to return to the same position in the sky.**

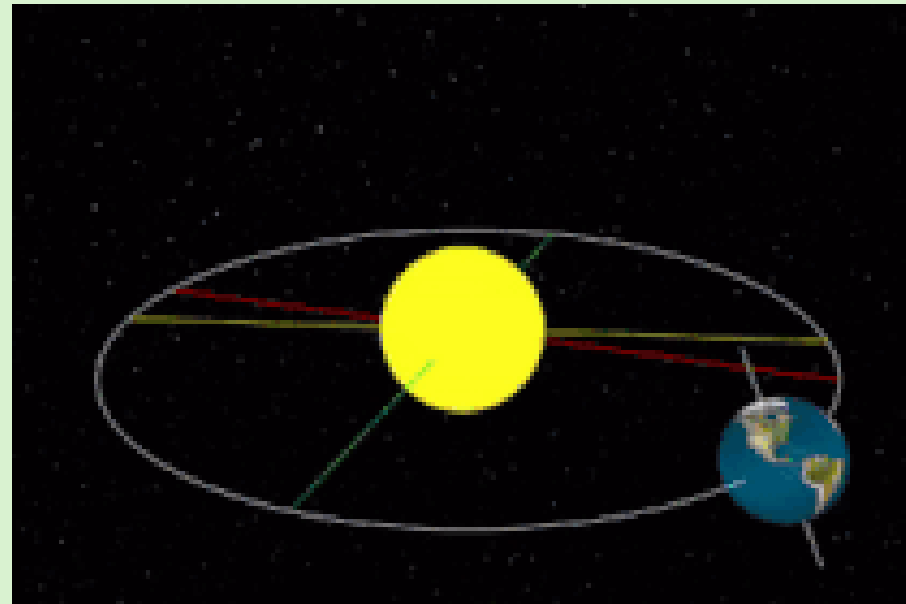


**Where's this difference coming from?**



# Where's this difference coming from?

- The day/night cycle due to Earth's rotation, has nothing to do with the yearly cycle from Earth's revolution.



# Where's this difference coming from?

- The tropical year is actually 365 days, 5 hours, 48 minutes, and 46 seconds long, or 365.242199 days long.



# Where's this difference coming from?

- The tropical year is actually 365 days, 5 hours, 48 minutes, and 46 seconds long, or 365.242199 days long.
- TBH, a day isn't exactly 24 hours long. But that's a story for another time.



**Before we dive in, why do we have seasons?**



**Reason for seasons:**





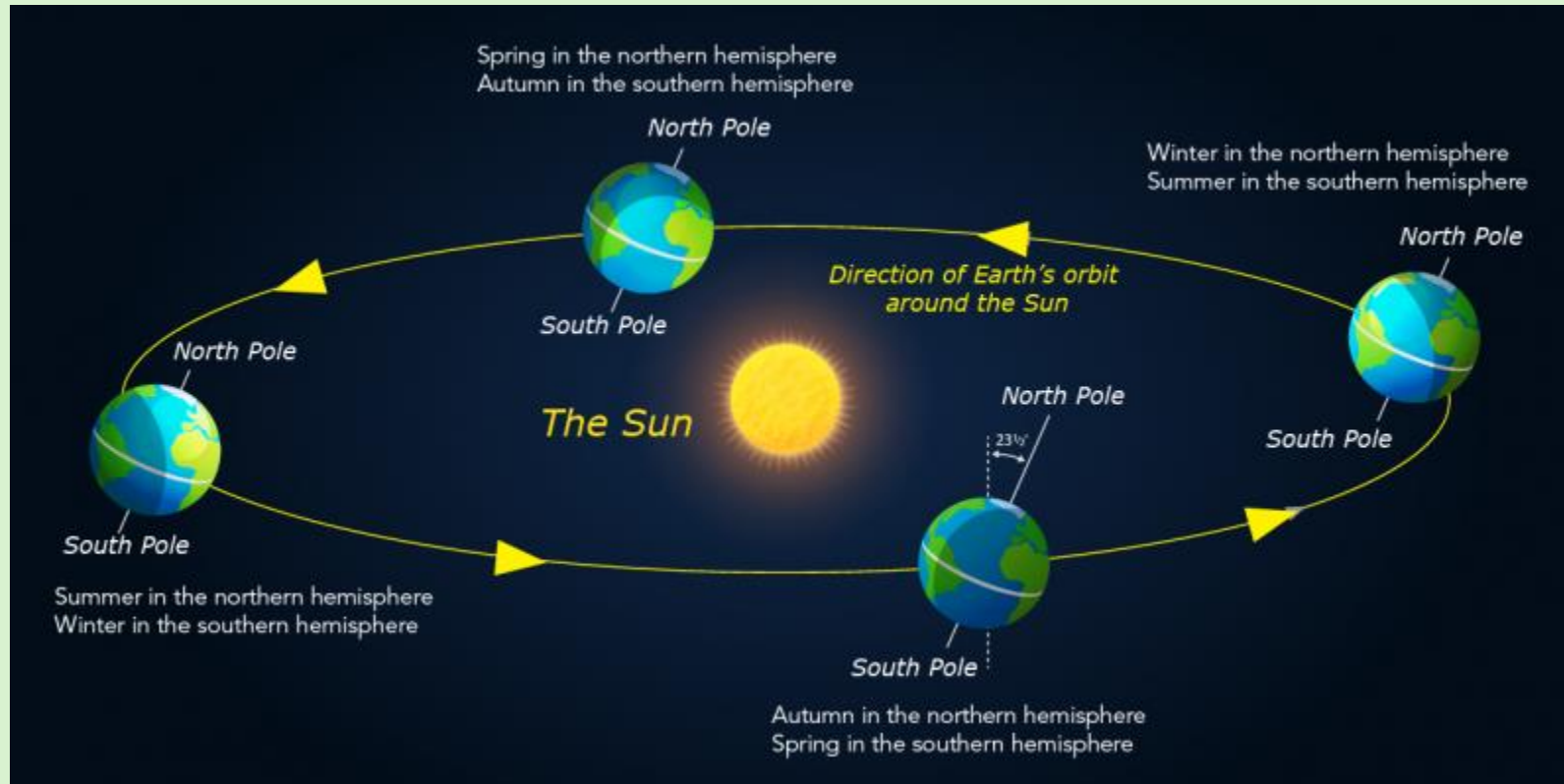
# Reason for seasons:

- Earth has seasons because something collided and caused the axial tilt.

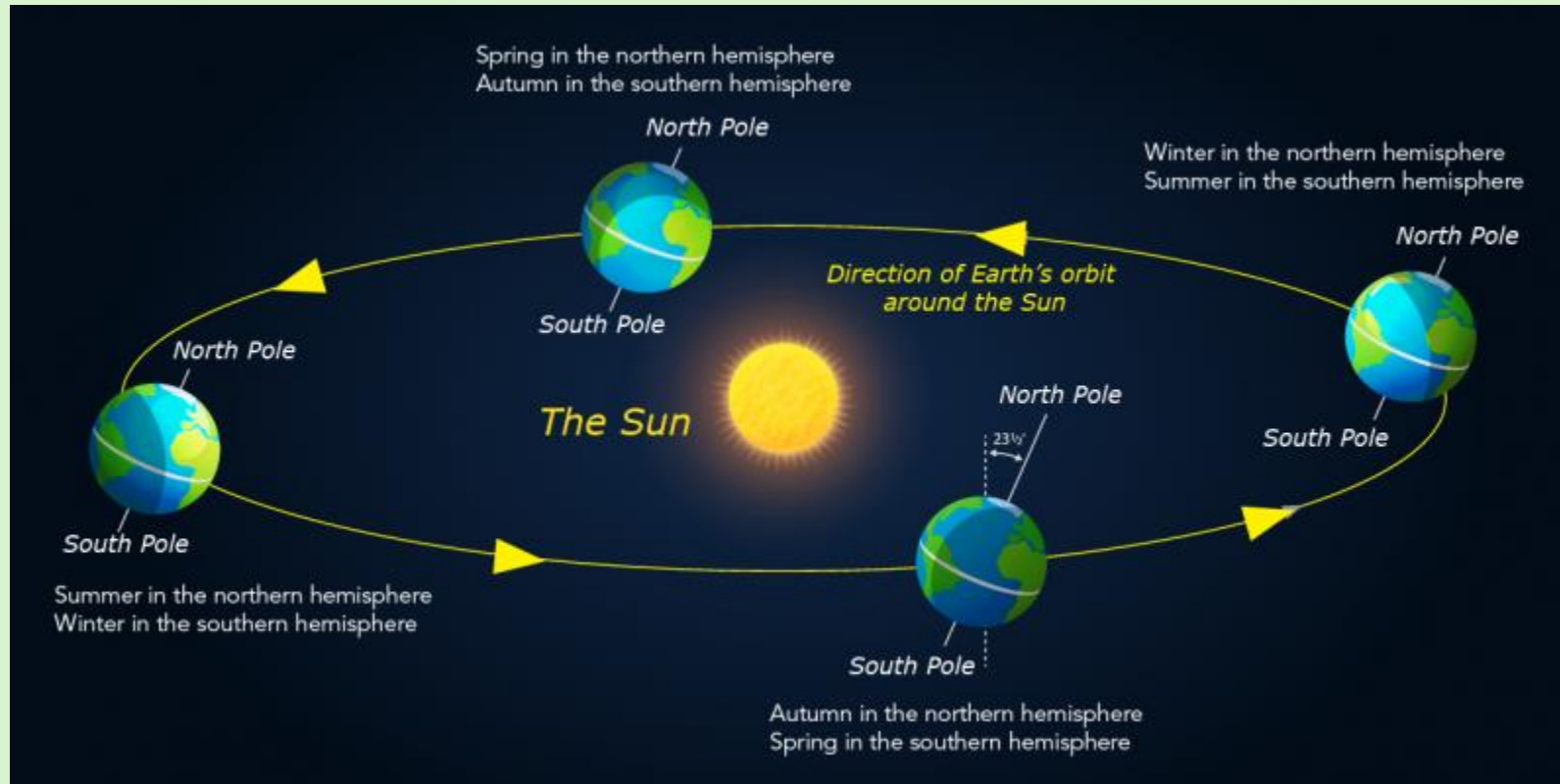




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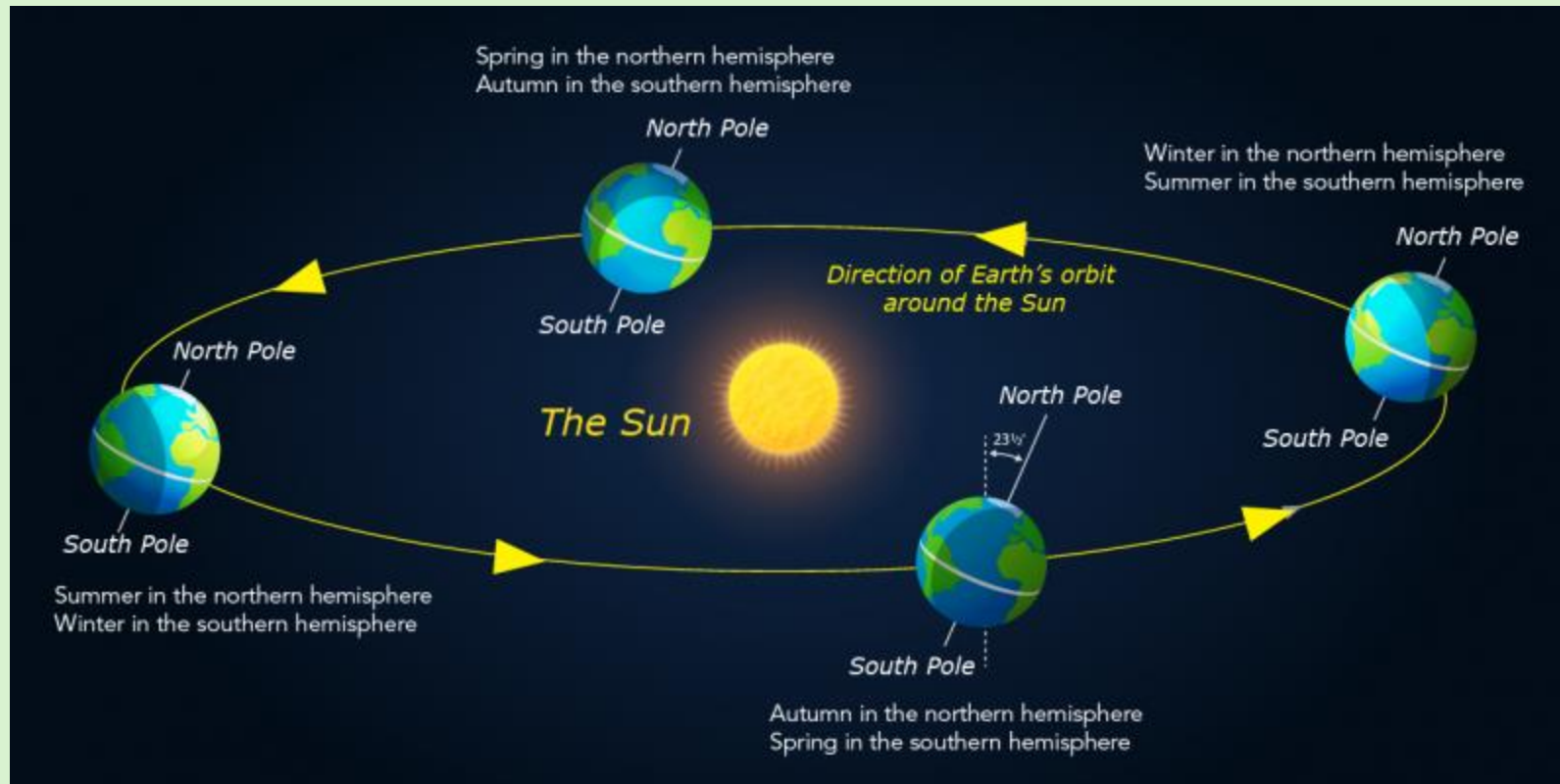


# What happens if we use 365 days?



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- Seasons go out of sync!



# What happens if we use 365 days?



# What happens if we use 365 days?

- The extra 0.24 days throws seasons off after a few years!





# What happens if we use 365 days?

- **Also, bad news for farmers!**



**How to solve this problem?**

# How to solve this problem?

- **Leap year!**



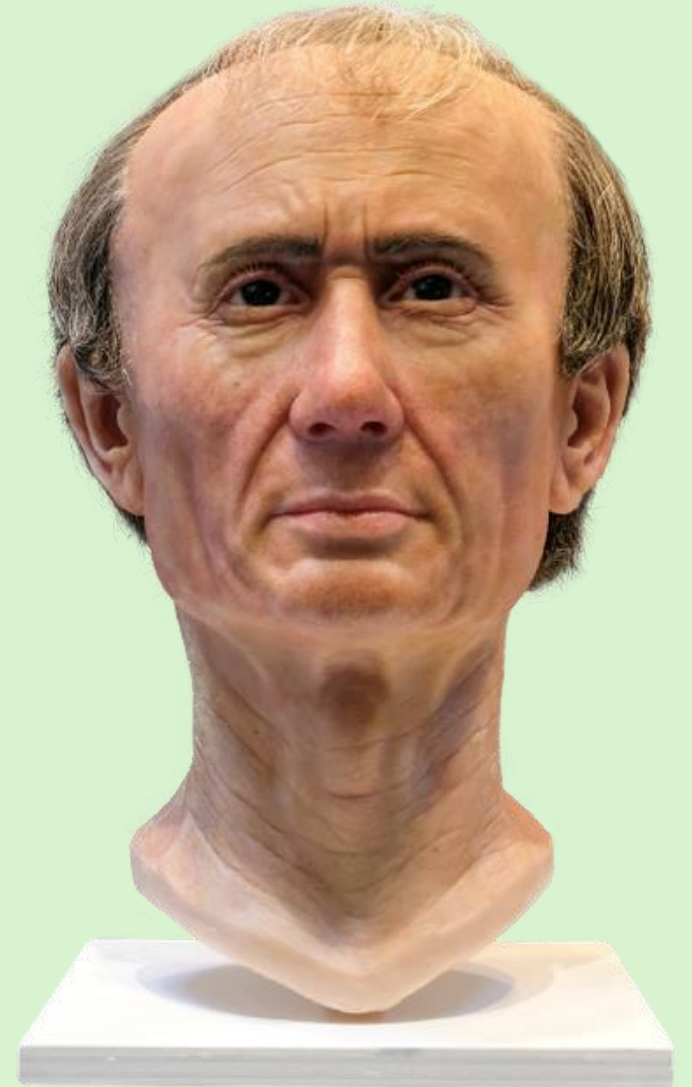
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- **Leap year!**
- **Egyptian astronomers around 50 B. C. measured the Earth's orbit to be close to 365.25 days long.**



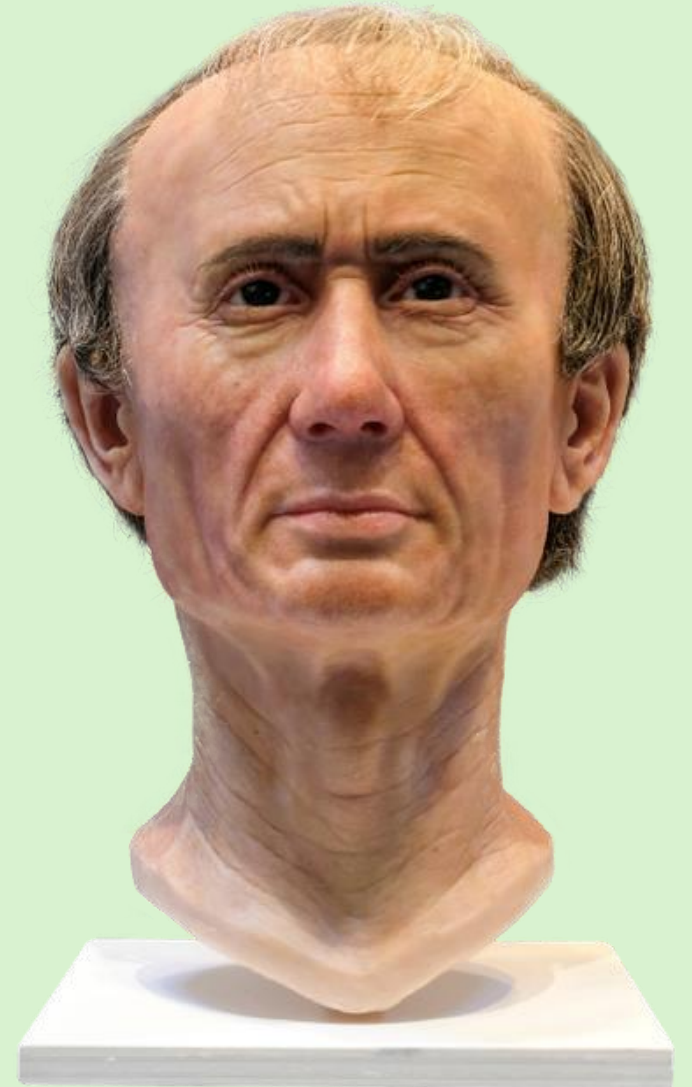
# How to solve this problem?

- **Leap year!**
- **Egyptian astronomers around 50 B. C. measured the Earth's orbit to be close to 365. 25 days long.**
- **Julius Caesar implemented a new calendar in 46 B. C. , adding one day every four years.**



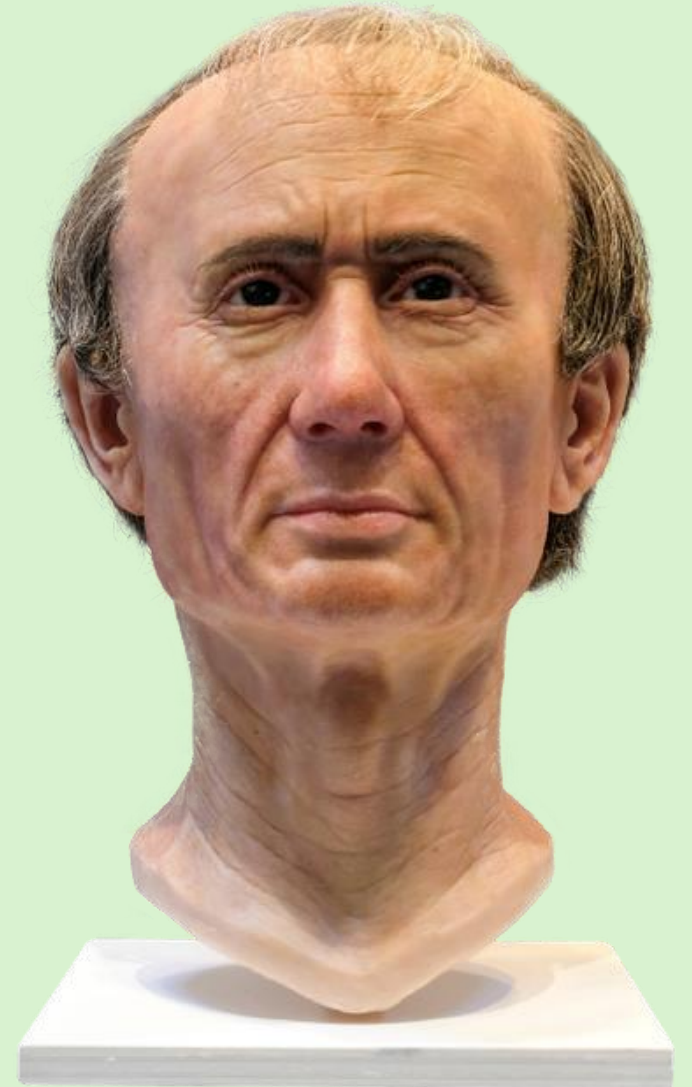
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- **Julius Caesar implemented a new calendar in 46 B. C. , adding one day every four years.**
- **Essentially adding it to the last month of the leap year.**
- **He also did a bunch of crazy stuff. .**



**What else did Caesar do?**



# What else did Caesar do?

- He shifted the beginning of the year from March 1 to January 1!





# What else did Caesar do?

- He also shifted the beginning of the year from March 1 to January 1!
- That's why the 7<sup>th</sup> month (September) through the 10<sup>th</sup> month (December) are now the 9<sup>th</sup> through 12<sup>th</sup> months.



# What else did Caesar do?

- He also shifted the beginning of the year from March 1 to January 1!
- That's why the 7<sup>th</sup> month (September) through the 10<sup>th</sup> month (December) are now the 9<sup>th</sup> through 12<sup>th</sup> months.
- February, the 'original' 12<sup>th</sup> month, now gets to be the 2<sup>nd</sup>, and that's the reason why we have the leap day this month.





**Problem solved?**

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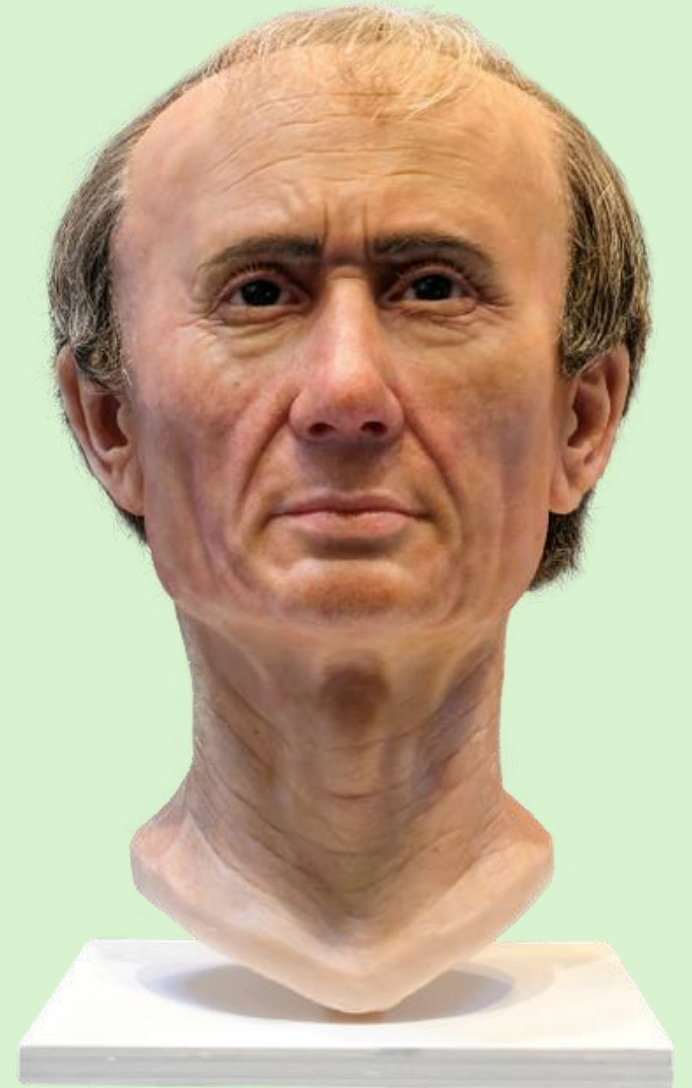


**Acshually..**



# Acshually. .

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- **Over four years, that adds up to 23 hours, 15 minutes, and 4 seconds.**
- **That's 44 minutes, 56 seconds less than a day.**
- **This adds about 3.12 days every 400 years.**





**Cut to late 1500s..**



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- **By 1582 A. D. , this added up to 12.7 days, pushing spring towards winter.**



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no.



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- **Pope Gregory XIII decreed a new calendar in October that year.**



# Cut to late 1500s. .

- By 1582 A. D. , this added up to 12.7 days, pushing spring towards winter.
- The Catholic Church did not want to celebrate Easter in winter.
- Pope Gregory XIII decreed a new calendar in October that year.
- But at what cost?



**New era begins. .**



# New era begins..

- Thursday, 4 October 1582, was followed by Friday, 15 October 1582, with ten days skipped.

# LVNARIO

## NOVO. SECONDO LA NVOVA RI- FORMA DELLA CORRETTIONE DEL LANNO.

RIFORMATO DA N. S. GREGORIO XIII.

Calcolato sotto il meridiano dell'Alma Città di Roma, per M. Eufebio de Alessandri Vercellese, nel quale  
oltre le congiuntioni, opposizioni, & quadrati della Luna con il Sole, vi si son poste ancora le feste  
mobili, & quelle di Palazzo, & di Campidoglio, & li giorni buoni per cauar sangue, & dar  
medicene, & serue per tre Mesi, cio è Ottobre, Nouembre, & Decembre.

Breue giuditio, sopra la stagione vernale, dell'Anno Riformato.

ALLI 12. di Decembre, secondo la Nuova Riforma, & correzione dell'Anno fatta per ordine di N. S. Papa Gregorio XIII. il Solstizio Vernale darà principio, perche il Sole ad Hore 10. minuti 24. del giorno medesimo perentrà al primo minuto di Capricorno, nel quale punto finirà l'Aurumno del Anno 82. & comincerà l'Inverno. Venere fortificata nel mezzo del Cielo, ottenendo il dominio già dell'Anno, & per esser ella di natura fredda, & humida, & per questa sua qualita, fara la stagione che fara alquanto humida, & la maggior parte fredda, non senza alcune pioggie. Purè le alcune desiderata fa più appieno del Giudicio dell'Anno prossimo del' 83. insieme co alcune influenze che minacciano il pianeta, per li varij aspetti ch'hanno tra d'essi per queste lor congiuntioni, anderà al mio Calcolo delle Congiuntioni, & Opposizioni del Sole con la Luna, & dell'altri pianeti fatto sopra l'Anno del 1583. Incominciando dal primo d'Ottobre, & lui vedrà le mutationi delle quattro stagioni dell'Anno, & in qual tempo, giorno, hora, & minuti, daranno principio i quattro punti Cardinali, & della solstij, & equinoctij, & secondo la nuova riforma dell'Anno. Di più ci sono le mutationi de i tempi & dell'Arafinense che il Sole giorno per giorno in ascendere sopra il nostro orizzonte, con vn bellissimo auuercimento che si deue offerare di per di, per dar medicene & andar alla stoffa, & à i bagni, & secondo i buoni & tristi Aspetti de gli pianeti, & far altre operationi, come lui se potrà meglio vider, & ancora la quantita dell'hore del giorno.

Ottobre lettera Dñicale G.

Nouembre hà giorni 30.

Decembre hà giorni 31.

D.	H.	M.	
1	1	1	Luna Piena
2	2	2	buono per andar alla stoffa
3	3	3	
4	4	4	S. Francesco confid.
5	5	5	
6	6	6	16 triba per stoffa
7	7	7	17 On-her-luora. Dñale. C.
8	8	8	18 primo quarto
9	9	9	19 bono per stoffa
10	10	10	20 bono per stoffa
11	11	11	21 vltimo per stoffa
12	12	12	22 vltimo per stoffa
13	13	13	23
14	14	14	24
15	15	15	25 Luna nuova
16	16	16	26
17	17	17	27
18	18	18	28
19	19	19	29 bono per stoffa
20	20	20	30 bono per stoffa
21	21	21	
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D.	H.	M.	
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OTTOBRE.

NOVEMBRE.

DECEMBRE.

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Con Licentia delle Superiori.

In Roma Appresso Vincenzio Accolti.

1582.

& permisso Ant. Lili.

# New era begins. .

- **Thursday, 4 October 1582, was followed by Friday, 15 October 1582, with ten days skipped.**
- **Understandably, people were pissed.**



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- **Understandably, people were pissed.**
- **But the problem of overcorrection persists.**
- **How do we correct that?**



**New formula:**

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- Rinse and repeat the same trick!





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# New formula:

- Remember the 3. 12 days added every 400 years?
- Rinse and repeat the same trick!
- They designated only certain hundred-year dates as leap years.
- Only hundred-year dates such as 1600, 2000, etc. which are divisible by 400 are leap years.
- Others, such as 1700, 1800, 1900, 2100, etc. are not!



**Is it perfect?**

# Is it perfect?

- **Not really; but will work for a long time ~ 3333.3 years.**



**More math! Why 3333. 3 years?**

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# Anyway. .

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- $12 - 3 = 9$ , so we actually have  $300 - 9 = 291$  leap years. And  $1200 - 291 = 909$  regular years.



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- The average length of year becomes  $(291 \times 366 + 909 \times 365)/1,200 = 365.2425$  days.



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- The average length of year becomes  $(291 \times 366 + 909 \times 365)/1,200 = 365.2425$  days.
- This gives an error of  $365.2425 - 365.2422 = 0.0003$  days per year, or one day every 3,333.3 years.



**What next?**

# What next?

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- **Therefore, we will need new calculations to correct for those changes.**



# What next?

- **Earth's rotation and revolution are changing constantly.**
- **Therefore, we will need new calculations to correct for those changes.**
- **Current astronomers don't really care, it is up to the future astronomers to figure it out.**



**Questions?**





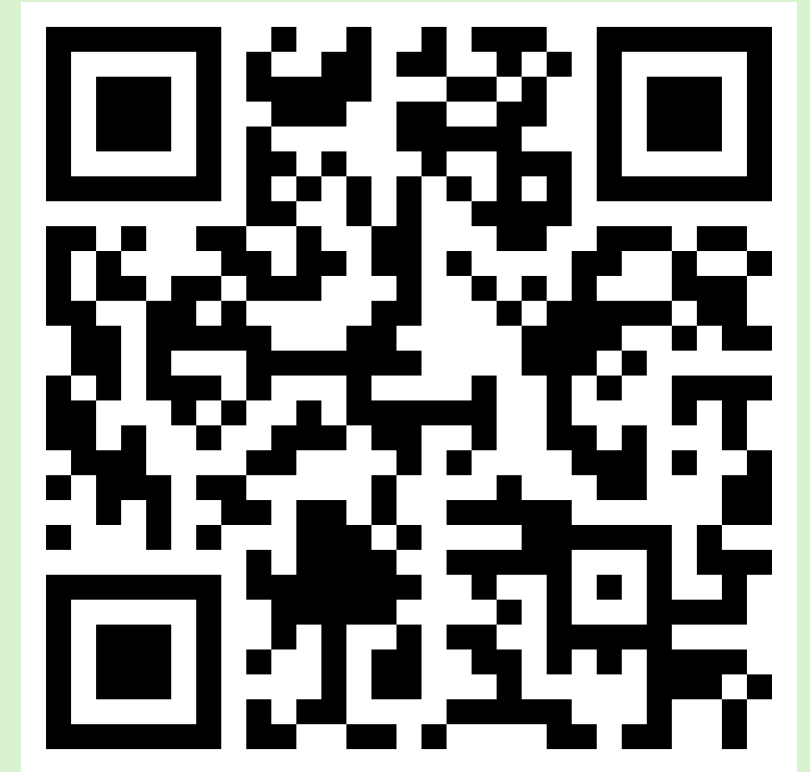
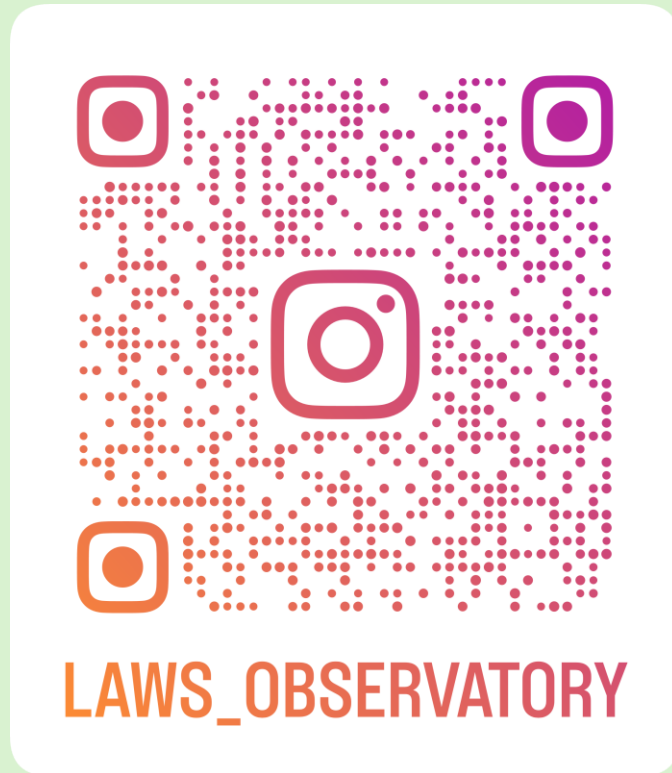
# April 8th Eclipse: ~94% in Columbia



**Info from  
NASA:**

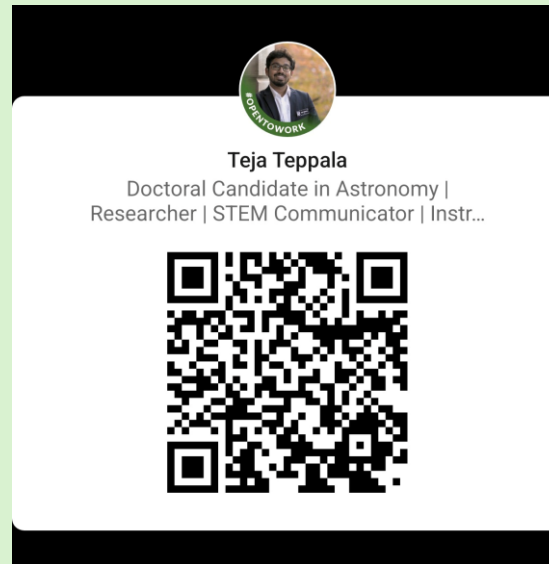


# Follow Laws Observatory:



# Thank you!

- Teja Teppala
- [ttgbk@mail.missouri.edu](mailto:ttgbk@mail.missouri.edu)



**ECLIPSE**  
**AMBASSADORS**





# How did Egyptian astronomers figure the length of Earth's orbit?

- Egyptians started out with a lunar calendar, based on Moon's phases.
- It was around 354 days long (loss of 11 days).
- Around 2500 B. C. , they adopted a new “civil” calendar based upon astronomical observations of Sirius.
- Sirius appeared right before sunrise around the onset of Nile's flood.



# How did Egyptian astronomers figure the length of Earth's orbit?

- They tried to correct it based on Sirius' reappearance during the next flooding.
- This ended up in a calendar year of 365 days; 12 months of 30 days each and a "13<sup>th</sup> month" of 5 days.
- Over time, they realized that Sirius rose a day late every 4 years.
- Thus, they figured that the actual year is a quarter day longer than 365 days.

